

Bifurcation of Polyelectrolyte Brushes Subject to Normal Electric Fields

Tyler N. Shendruk

Yu-Fan Ho Gary W. Slater Pai-Yi Hsiao

CAP

May 31, 2013



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Stimuli-Responsive MEMS Components

"Smart" Surfaces



Stimuli-Responsive Materials

Polyelectrolyte Brushes

Perpendicular Fields

Simulations

Low Grafting Density

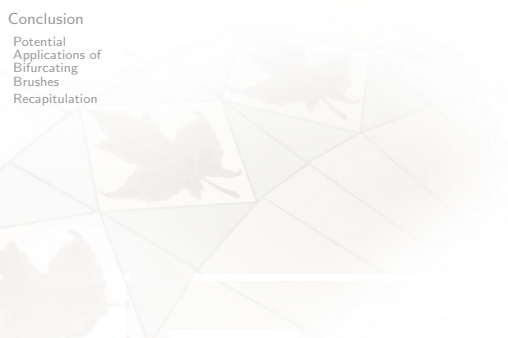
Intermediate Grafting Density

High Grafting Density

Conclusion

Potential Applications of Bifurcating Brushes
Recapitulation

- Biology abounds with mesoscopic systems that dynamically and reversibly respond to environmental cues



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Schematic of biological and synthetic, mechanically triggered stimuli-responsive surfaces
Credit: Wilhelm Huck, Melville Laboratory for Polymer Synthesis

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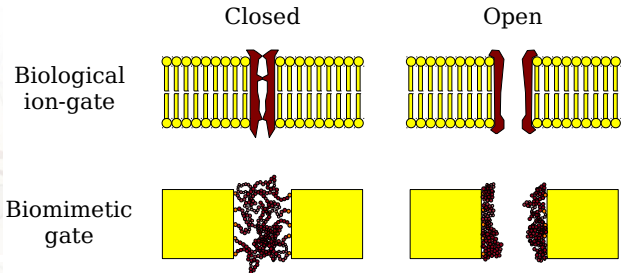
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- Biology abounds with mesoscopic systems that dynamically and reversibly respond to environmental cues
- If structures change radically with environment they can be engineered into
 - detectors
 - *gates*



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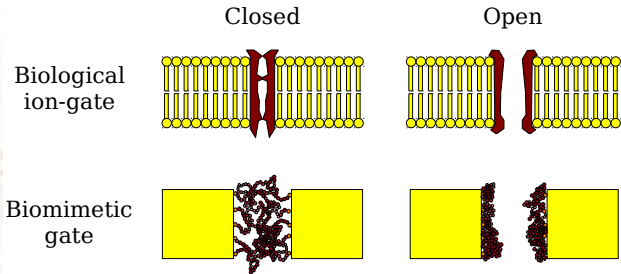
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Charged Soft Matter as “Smart” Surfaces

Polyelectrolyte Brushes



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Recapitulation

- Different than neutral brush due to *chain-counterion complex* nature
- f is charge fraction of chain, z valency, N number of segments, H brush height, T counterion cloud thickness and Σ normalized grafting density



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- f is charge fraction of chain, z valency, N number of segments, H brush height, T counterion cloud thickness and Σ normalized grafting density
- Ideal as stimuli-responsive surfaces because structure is *hyper-dependent* on environmental cues



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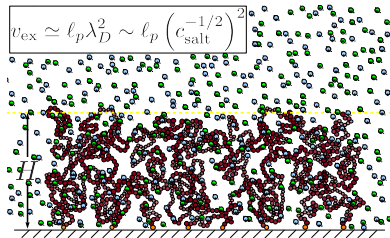
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High Salt Brush

- Salt screens electrostatics so brush is effectively electro-*neutral*
 - Screening inverse to salt concentration
 - $H \sim N$
 - $H \sim \Sigma^{1/3}$



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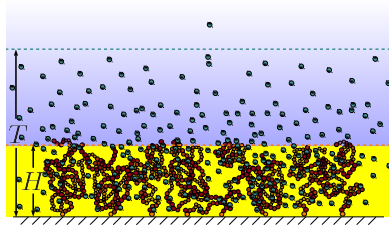
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Pincus Brush (weakly charged)

- Brush is like a *thin charged film* and counterion cloud is attracted to it
 - $T \sim [\Sigma N]^{-1}$
 - $H \sim N^3$ — strong dependence
 - $H \sim \Sigma$



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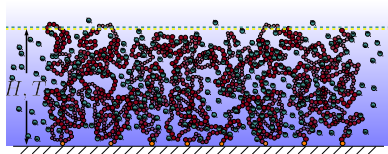
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Osmotic Brush (highly charged)

- Counterions are pulled into brush (polyelectrolyte / counterion complex)
 - $T \approx H$
 - $H \sim N$
 - H does not have Σ dependence



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Osmotic Brushes as “Smart” Surfaces

- Ideal as stimuli-responsive surfaces because structure is *hyper-dependent* on environmental cues
- Favourable because form electroneutral films when unperturbed
- Easy, reproducible control over switching:
 - temperature
 - salt
 - pH



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Osmotic Brushes as “Smart” Surfaces

- Ideal as stimuli-responsive surfaces because structure is *hyper-dependent* on environmental cues
- Favourable because form electroneutral films when unperturbed
- Easy, reproducible and *fast* control over switching:
 - temperature
 - salt
 - pH
 - *electric fields*



Langevin Dynamics

Simulations of Polyelectrolyte Brushes Subject to Normal Electric Fields



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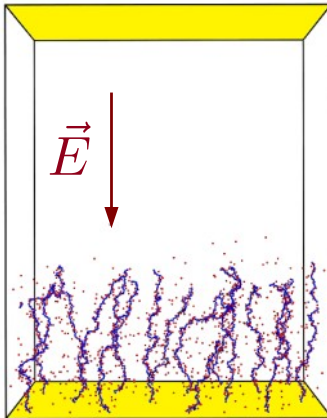
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Modeling the separation of macromolecules: A review of current computer simulation methods.
Electrophoresis, 30: 792-818, 2009.

Langevin Dynamics

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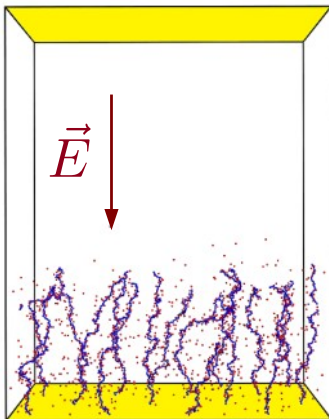
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- Low Grafting Density:
 $\Sigma = 0.0136$
- Intermediate Grafting Density:
 $\Sigma = 1.11$
- High Grafting Density:
 $\Sigma = 11.1$

Low Grafting Density



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Low Grafting Density Brushes Subject to Normal Electric Fields



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Low Grafting Density Brush Height



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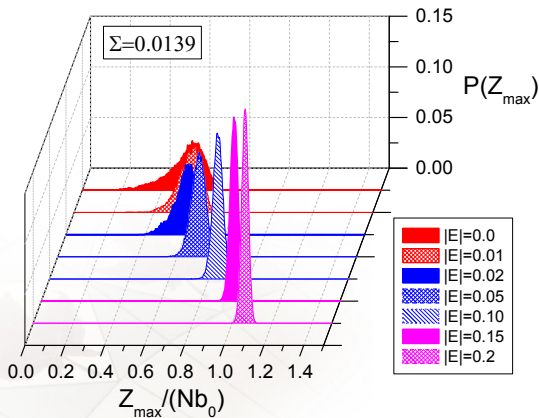
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Low Grafting Density Brush Height



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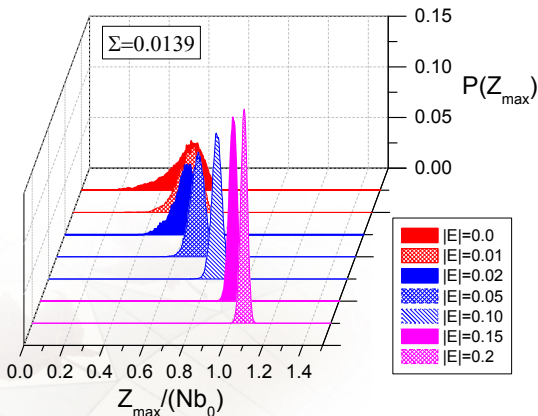
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Two regimes:

- $|E| \lesssim 0.02$:
Height is rather
constant



Low Grafting Density Brush Height



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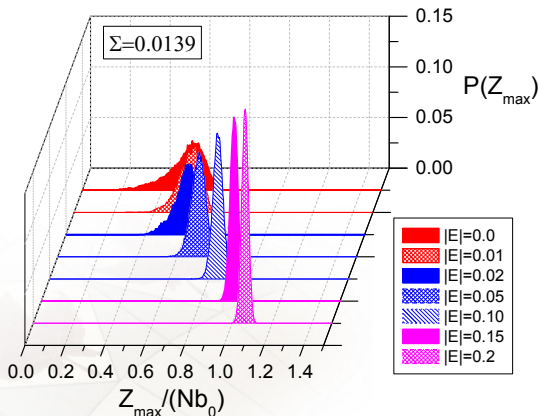
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Two regimes:

- $|E| \lesssim 0.02$:
Height is rather constant
- $|E| \gtrsim 0.02$:
Height increases with increased $|E|$



Low Grafting Density Brush Height



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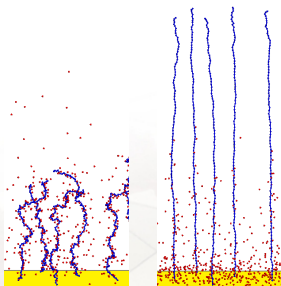
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Two regimes:

- Why not a steady rise?
- What does “critical” $|E^*|$ arise from?



Low Grafting Density

Monomer/Counterion Distributions — Low Fields



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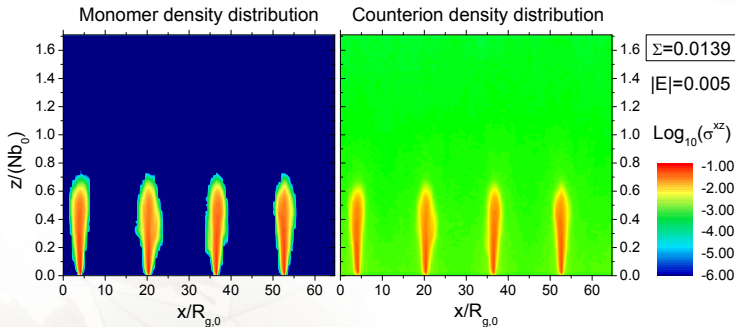
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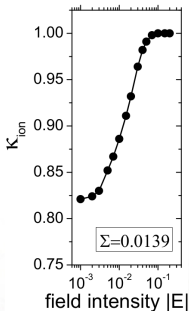


- Counterion distribution corresponds to monomer distribution
- Not perfectly electroneutral — background probability
- Low grafting density brush not quite *ideal osmotic brush*



Low Grafting Density

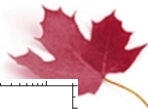
Counterion Confinement and Condensation



In weak field limit, 82% of counterions *confined to brush region* ($z \leq Z_{max}$)

Low Grafting Density

Counterion Confinement and Condensation



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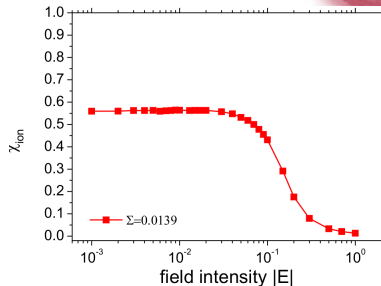
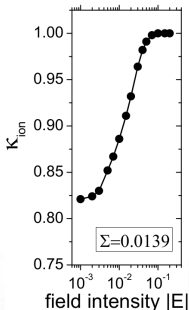
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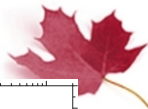
In weak field limit, 82% of counterions *confined to brush region* ($z \leq Z_{\text{max}}$)

- 56% *condensed* (closer than λ_B to a chain)
- Manning theory for free chain predicts $\chi_{\text{ion}} = 1 - b_0/\lambda_B = 61\%$



Low Grafting Density

Counterion Confinement and Condensation



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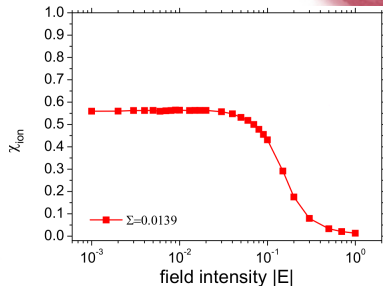
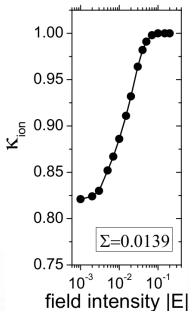
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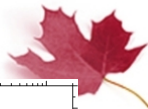
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Although not perfect, screening is effective for fields $\lesssim |E^*| \simeq 0.02$



Low Grafting Density

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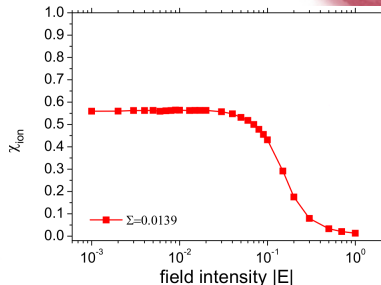
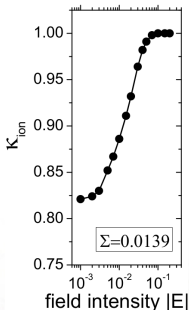
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Although not perfect, screening is effective for fields $\lesssim |E^*| \simeq 0.02$

- When $|E| \ll |E^*|$, counterion and monomer distributions correspond
- When $|E| \gtrsim |E^*|$, counterions forced down thus superimposing exponential/Boltzmann distribution
- When $|E| \gg |E^*|$, positive monomers hardly perturb exponential distribution



Low Grafting Density Critical Field



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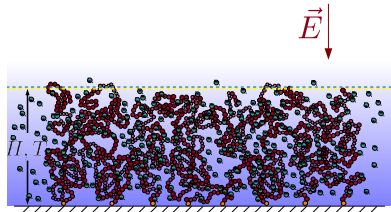
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Scaling Argument

Chain stretches once energy gained by moving charge a *characteristic distance*, ℓ , is greater than $k_B T$

$$E^* e \ell \sim k_B T \quad \rightarrow \quad E^* \sim \frac{k_B T}{e} \frac{1}{\ell}$$



Low Grafting Density Critical Field



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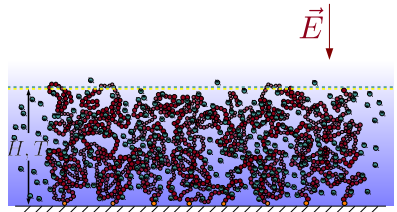
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But what is the *characteristic distance*?



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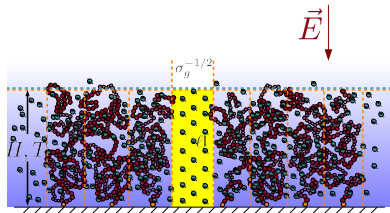
Chain stretches once energy gained by moving charge a *characteristic distance*, ℓ , is greater than $k_B T$

$$E^* e \ell \sim k_B T \quad \rightarrow \quad E^* \sim \frac{k_B T}{e} \frac{1}{\ell}$$

But what is the *characteristic distance*?

- In mean-field sense, ℓ is average distance between charges

$$\ell \sim \left(\frac{H \sigma_g^{-1}}{N} \right)^{1/3}$$



Low Grafting Density Critical Field



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Scaling Result

$$E^* \sim \frac{k_B T}{e} \left(\frac{N \sigma_g}{H} \right)^{1/3}$$

$$\sim \Sigma^{1/3}$$



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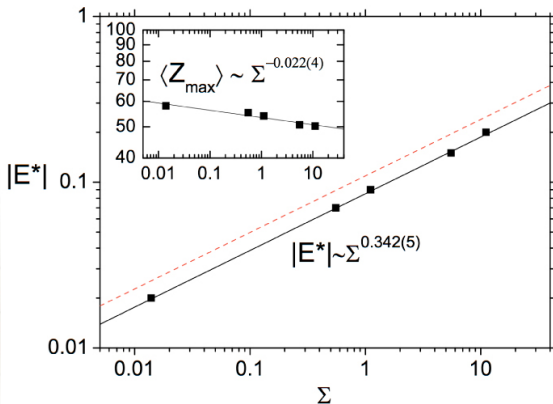
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Scaling Result

$$E^* \sim \frac{k_B T}{e} \left(\frac{N \sigma_g}{H} \right)^{1/3} \sim \Sigma^{1/3}$$



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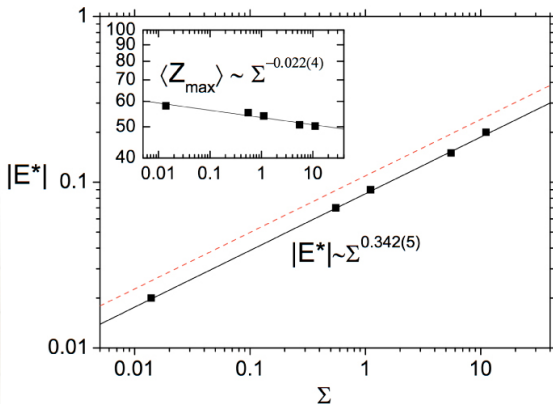
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Scaling Result

$$E^* \sim \frac{k_B T}{e} \left(\frac{N \sigma_g}{H} \right)^{1/3}$$

$$\sim \Sigma^{1/3}$$

- If $H = H(\Sigma)$ (as observed) then $E^* \sim \Sigma^{0.341}$.



Low Grafting Density

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Conclusion About Low Grafting Density:

- There are two regimes:
 - $|E| < |E^*|$: brush height is constant
 - $|E| > |E^*|$: brush height increases
- $E^* \sim \Sigma^{1/3}$



Intermediate Grafting Density



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Intermediate Grafting Density Brushes Subject to Normal Electric Fields



Intermediate Grafting Density

Brush Height



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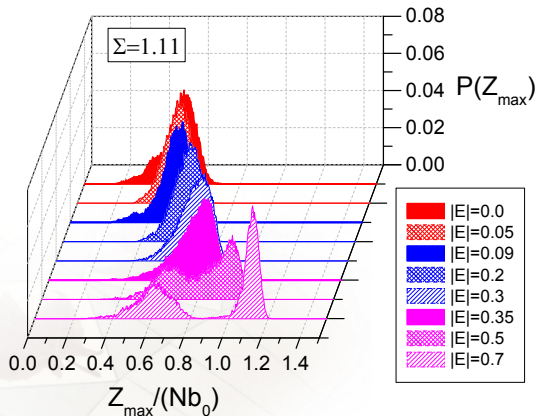
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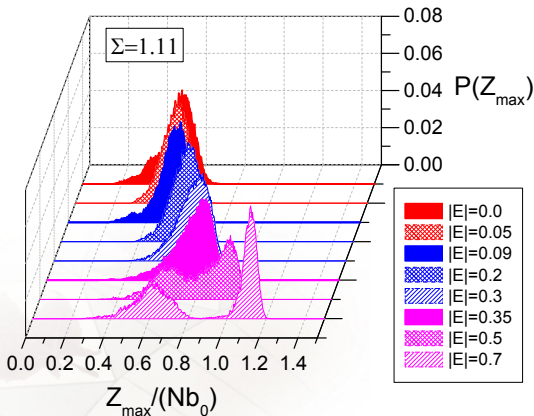
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Three regimes:

- Height constant at low fields
 $|E^*| \simeq 0.09$
- Height increases at intermediate fields



Intermediate Grafting Density

Brush Height



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Simulations

Low Grafting
Density

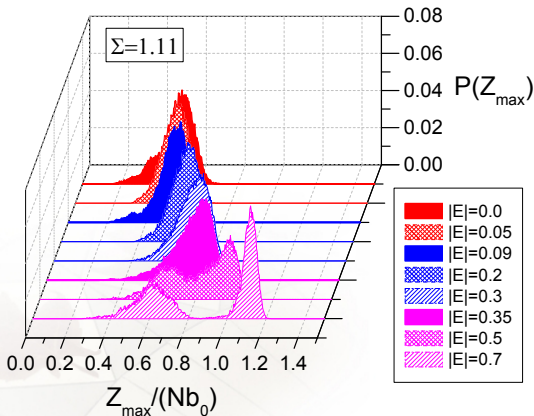
Intermediate
Grafting
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High Grafting
Density

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Three regimes:

- Height constant at low fields
 $|E^*| \simeq 0.09$
- Height increases at intermediate fields
- Splitting at *second critical field*
 $|E^{**}| \simeq 0.35$



Intermediate Grafting Density

Monomer/Counterion Distributions — Low Fields



Stimuli-
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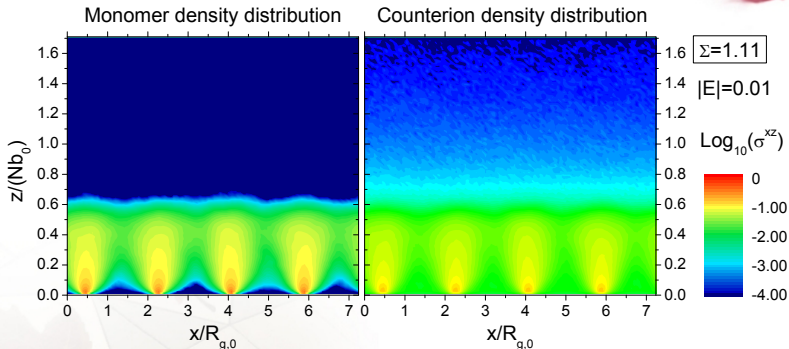
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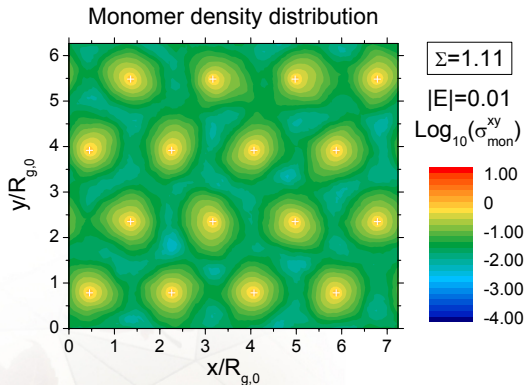


- At intermediate densities brush is closer to ideally *osmotic*
- Most (97% in zero field) counterions reside within brush
- More homogeneous and effectively electroneutral



Intermediate Grafting Density

Monomer/Counterion Distributions — Low Fields

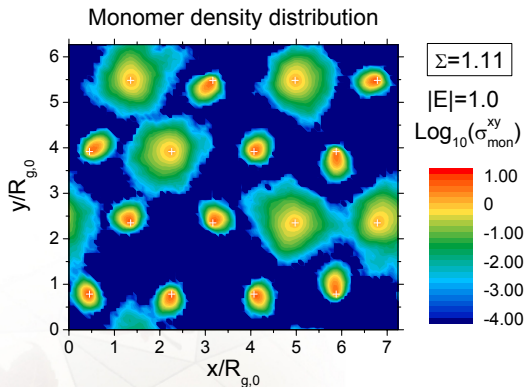


- At intermediate densities brush is closer to ideally *osmotic*
- Most (97% in zero field) counterions reside within brush
- More homogeneous and effectively electroneutral



Intermediate Grafting Density

Monomer/Counterion Distributions — High Fields



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Intermediate Grafting Density

Monomer/Counterion Distributions — High Fields



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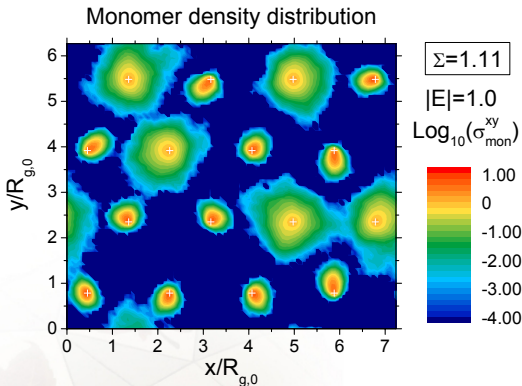
Low Grafting
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- The population bifurcates into
 - few unstretched chains
 - many highly stretched chains



Intermediate Grafting Density

Brush Height – Bifurcation



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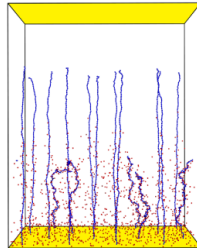
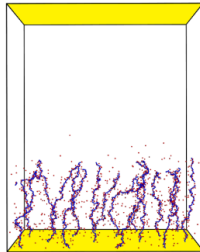
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- Why does *bifurcation* occur at $|E^{**}|$?

Intermediate Grafting Density Critical Field



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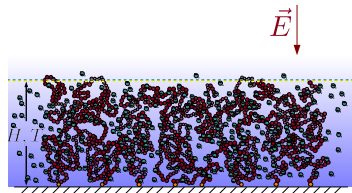
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Scaling Argument

Second critical field $|E^{**}|$ is the minimum for which



Intermediate Grafting Density Critical Field



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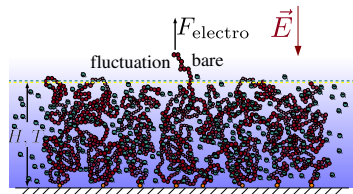
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Scaling Argument

Second critical field $|E^{**}|$ is the minimum for which $F_{\text{electro}} = zqE$ on segment that has fluctuated out of the protective counterion cloud



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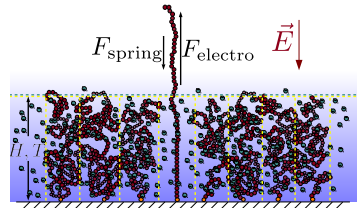
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Scaling Argument

Second critical field $|E^{**}|$ is the minimum for which $F_{\text{electro}} = zqE$ on segment that has fluctuated out of the protective counterion cloud is greater than the elastic restoring force $F_{\text{spring}} = H/Na^2$



Intermediate Grafting Density Critical Field



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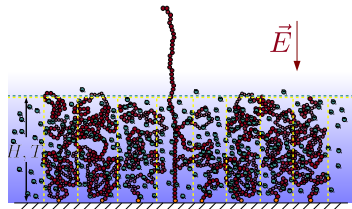
Scaling Argument

Second critical field $|E^{**}|$ is the minimum for which $F_{\text{electro}} = zqE$ on segment that has fluctuated out of the protective counterion cloud is greater than the elastic restoring force $F_{\text{spring}} = H/Na^2$

$$zqE^{**} \sim \frac{H}{Na^2}$$

$$E^{**} \sim \frac{1}{qa} \left(\frac{f}{z^3} \right)^{1/2} = \text{const.}$$

since $H \simeq Na(f/z)^{1/2}$ in an osmotic brush.



Intermediate Grafting Density Critical Field



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Scaling Argument

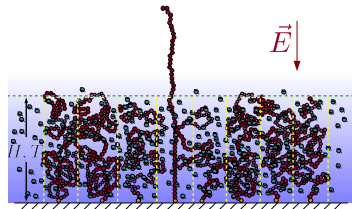
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$$E^{**} \sim \frac{1}{qa} \left(\frac{f}{z^3} \right)^{1/2} = \text{const.}$$

since $H \simeq Na(f/z)^{1/2}$ in an osmotic brush.

- E^{**} is not predicted to scale with Σ , nor N



Intermediate Grafting Density

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Conclusion About Intermediate Grafting Density:

- There are three regimes:
 - $|E^*| < |E|$: brush height is constant
 - $|E^*| < |E| < |E^{**}|$: brush height increases
 - $|E^{**}| < |E|$: brush *bifurcates*
- $|E^{**}| \sim \Sigma^0$



High Grafting Density



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High Grafting Density Brushes Subject to Normal Electric Fields



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High Grafting Density Immediate Bifurcation



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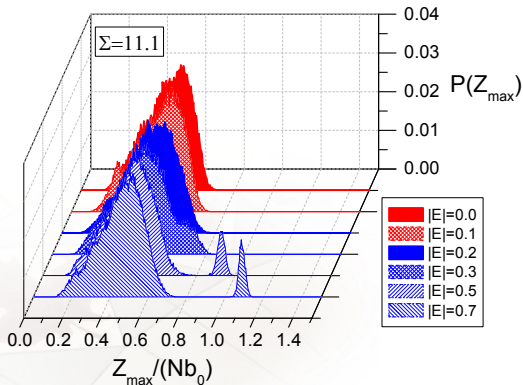
Low Grafting
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Bifurcates but ...

$$E^*(\Sigma) = E^{**} \text{ at high } \Sigma$$



High Grafting Density Immediate Bifurcation



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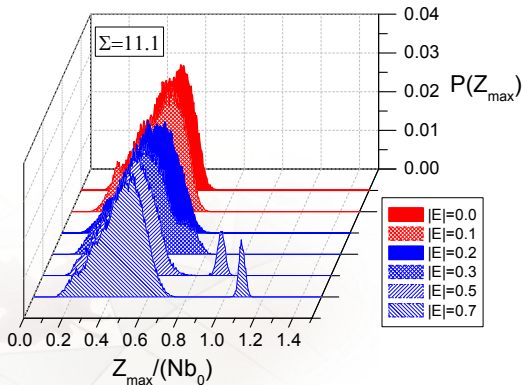
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Bifurcates but ...

$E^*(\Sigma) = E^{**}$ at high Σ

- Increasing Σ increases E^*
- but E^{**} nearly constant
- Therefore, *immediate* bifurcation at high Σ



High Grafting Density Immediate Bifurcation



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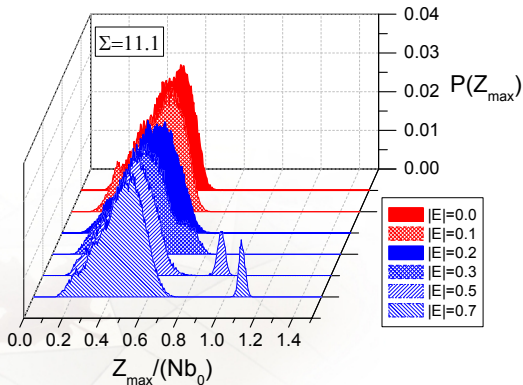
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Bifurcates but ...

$E^*(\Sigma) = E^{**}$ at high Σ

- Increasing Σ increases E^*
- but E^{**} nearly constant
- Therefore, *immediate* bifurcation at high Σ

Fully stretched chains now
the *minority*



High Grafting Density Minority



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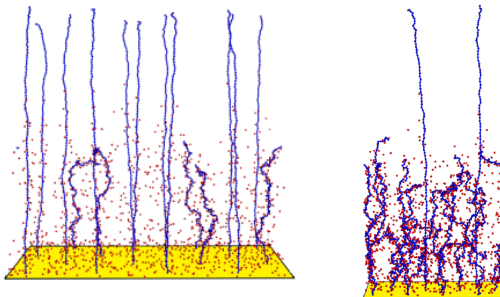
Low Grafting
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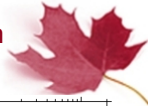


- When $|E| > |E^{**}|$:
Majority stretched if $\Sigma = 1.11$ but *minority* stretched if $\Sigma = 11.1$
- Why are more relaxed and unstretched compared to intermediate Σ ?



High Grafting Density

Increased Counterion Confinement and Condensation



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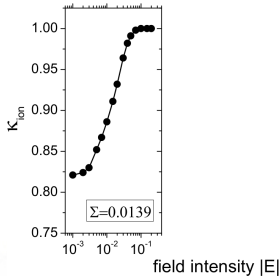
Intermediate
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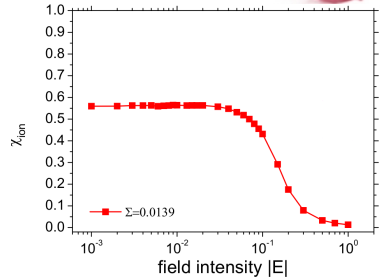
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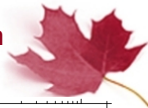
- In weak fields and low grafting density, 82% of counterions *confined* to brush



- In weak fields and low grafting density, 56% of counterions condensed

High Grafting Density

Increased Counterion Confinement and Condensation



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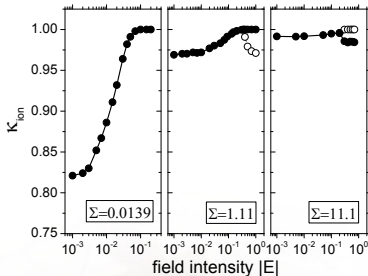
Low Grafting
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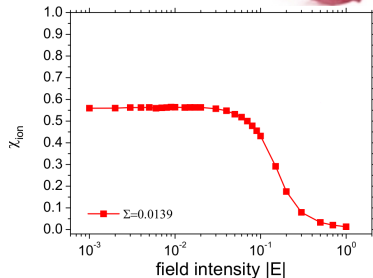
High Grafting
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- In weak fields and low grafting density, 82% of counterions *confined* to brush
- Jumps to 97% when $\Sigma = 1.11$ and 99% when $\Sigma = 11.1$

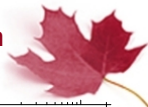


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High Grafting Density

Increased Counterion Confinement and Condensation



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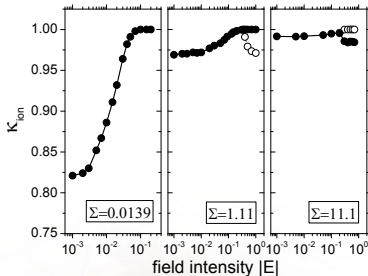
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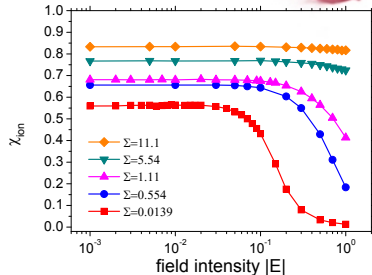
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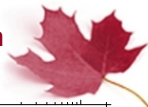


- In weak fields and low grafting density, 56% of counterions condensed
- Increases to 78% when $\Sigma = 1.11$ and 84% when $\Sigma = 11.1$

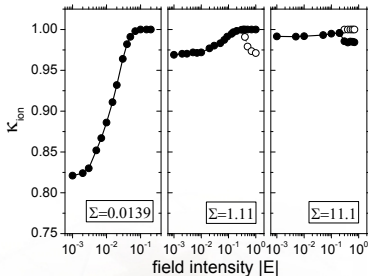


High Grafting Density

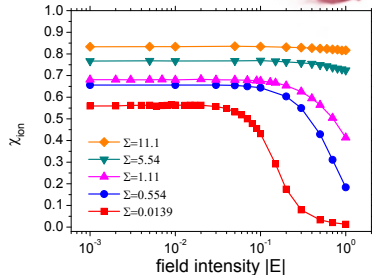
Increased Counterion Confinement and Condensation



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- In weak fields and low grafting density, 82% of counterions *confined* to brush
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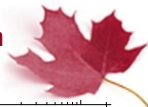


- In weak fields and low grafting density, 56% of counterions condensed
- Increases to 78% when $\Sigma = 1.11$ and 84% when $\Sigma = 11.1$

Assuming local neutrality becomes more accurate at higher grafting densities.

High Grafting Density

Increased Counterion Confinement and Condensation



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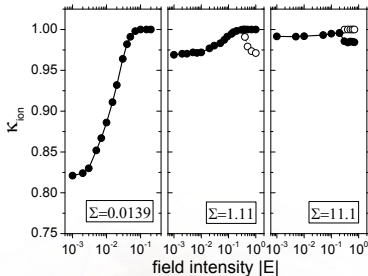
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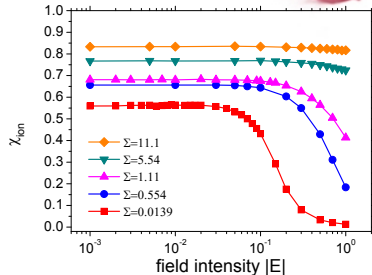
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- In weak fields and low grafting density, 82% of counterions *confined* to brush
- Jumps to 97% when $\Sigma = 1.11$ and 99% when $\Sigma = 11.1$



- In weak fields and low grafting density, 56% of counterions condensed
- Increases to 78% when $\Sigma = 1.11$ and 84% when $\Sigma = 11.1$

Assuming local neutrality becomes more accurate at higher grafting densities.

Less chains bare and liable to be fully stretched.



High Grafting Density

Conclusion



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Conclusion About High Grafting Density:

- At high grafting densities, $|E^*| = |E^{**}|$
- Fully stretched population becomes minority

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Potential Applications of Bifurcating Brushes



Original Motivation:

Polyelectrolyte brushes as field controlled gates

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Original Motivation:

Polyelectrolyte brushes as field controlled gates

but bifurcation suggests an array of unexpected possibilities.

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Original Motivation:

Polyelectrolyte brushes as field controlled gates
but bifurcation suggests an array of unexpected possibilities.

Novel MEMS Components:

- Control flow resistance

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Original Motivation:

Polyelectrolyte brushes as field controlled gates

but bifurcation suggests an array of unexpected possibilities.

Novel MEMS Components:

- Control flow resistance
- Filtration by number of rods

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Potential Applications of Bifurcating Brushes



Original Motivation:

Polyelectrolyte brushes as field controlled gates
but bifurcation suggests an array of unexpected possibilities.

Novel MEMS Components:

- Control flow resistance
- Filtration by number of rods
- Control the surface friction

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Original Motivation:

Polyelectrolyte brushes as field controlled gates

but bifurcation suggests an array of unexpected possibilities.

Novel MEMS Components:

- Control flow resistance
- Filtration by number of rods
- Control the surface friction
- Utilizing polyampholytes or end-labeled chains may allow choosing which chains stretch



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Original Motivation:

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but bifurcation suggests an array of unexpected possibilities.

Novel MEMS Components:

- Control flow resistance
- Filtration by number of rods
- Control the surface friction
- Utilizing polyampholytes or end-labeled chains may allow choosing which chains stretch
- *Fishing* – the tethering and subsequent trapping within the interior of the brush of analytes by alternating fields



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- Mykyta Chubynsky
- Henk de Haan
- Martin Bertrand
- Yuguo Tao
- David Sean
- Zheng Ma

Webpages

- Gary Slater:
www.science.uottawa.ca/~gslater
- Tyler Shendruk:
www.tnshendruk.com

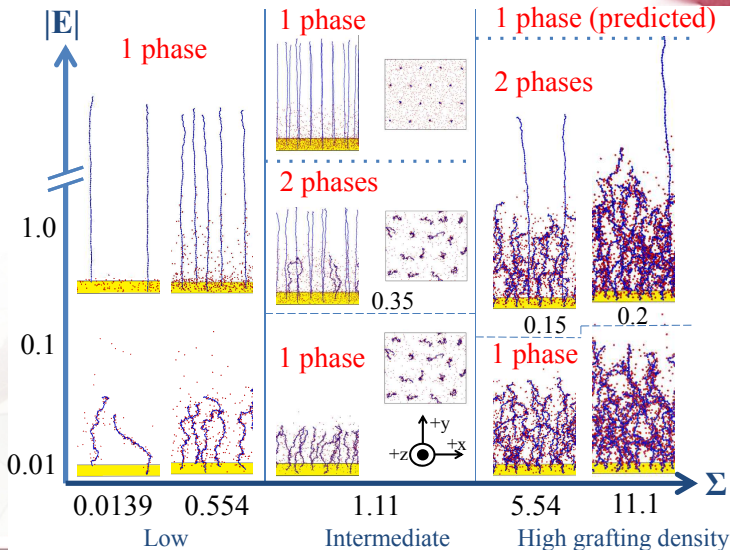


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Structure of polyelectrolyte brushes subject to normal electric fields.
Langmuir, 29(7): 2359-2370, 2013.

Recapitulation

Structure of *highly charged* polyelectrolyte brushes in the *no-salt* limit, subject to *normal electric fields*:



Structure of polyelectrolyte brushes subject to normal electric fields.
Langmuir, 29(7): 2359-2370, 2013.